

FIITJEE - JEE (Main)

PHYSICS, CHEMISTRY & MATHEMATICS

JEE Main 2019 Mock Tests-1 (Code:100312.1)

ANSWER KEY

PHYSICS (PART-I)

- | | | | |
|-------|-------|-------|-------|
| 1. B | 2. A | 3. C | 4. C |
| 5. C | 6. A | 7. C | 8. C |
| 9. B | 10. A | 11. D | 12. B |
| 13. A | 14. D | 15. B | 16. D |
| 17. B | 18. D | 19. B | 20. D |
| 21. D | 22. D | 23. A | 24. C |
| 25. B | 26. D | 27. C | 28. C |
| 29. C | 30. B | | |

CHEMISTRY (PART-II)

- | | | | |
|-------|-------|-------|-------|
| 1. B | 2. D | 3. C | 4. C |
| 5. C | 6. C | 7. B | 8. C |
| 9. A | 10. A | 11. C | 12. A |
| 13. A | 14. A | 15. D | 16. C |
| 17. B | 18. B | 19. C | 20. A |
| 21. A | 22. B | 23. B | 24. A |
| 25. A | 26. A | 27. D | 28. D |
| 29. D | 30. B | | |

MATHEMATICS (PART-III)

- | | | | |
|-------|-------|-------|-------|
| 1. C | 2. B | 3. A | 4. A |
| 5. B | 6. A | 7. C | 8. D |
| 9. A | 10. B | 11. A | 12. B |
| 13. B | 14. A | 15. C | 16. C |
| 17. D | 18. D | 19. A | 20. C |
| 21. B | 22. C | 23. C | 24. D |
| 25. C | 26. C | 27. C | 28. A |
| 29. D | 30. A | | |

HINTS AND SOLUTIONS

PHYSICS (PART-I)

1. Angle between P_1 and $P_2 = 30^\circ$ (given)
 Angle between P_2 and $P_3 = \theta = 90^\circ - 30^\circ = 60^\circ$
 $I_0 = 32 \text{ Wm}^2$
 The intensity of light transmitted by P_2 is $I_1 = \frac{I_0}{2} = \frac{32}{2} = 16 \text{ Wm}^{-2}$

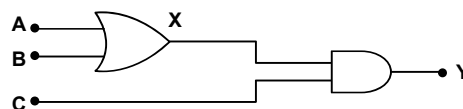
According to Malus law the intensity of light transmitted by P_2 is $I_2 = I_1 \cos^2 30^\circ = 6 \left(\frac{\sqrt{3}}{2} \right)^2 = 12 \text{ Wm}^{-2}$

Similarly intensity of light transmitted by P_2 is

$$I_3 = I_2 \cos^2 \theta = 12 \cos^2 60^\circ = 12 \left(\frac{1}{2} \right)^2 = 3 \text{ Wm}^{-2}.$$

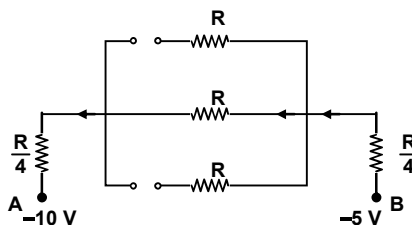
2. The film appears bright when the path difference ($2 \mu t \cos r$) is equal to odd multiple of $\frac{\lambda}{2}$.
 I.E., $2 \mu t \cos r = (2N - 1) \lambda/2$ WHERE $N = 1, 2, 3, \dots$
 $\therefore \lambda = \frac{4 \mu t \cos r}{(2n-1)} = \frac{56000}{(2n-1)} \text{ \AA}.$

- 3.
- | A | B | C | X=(A+B) | Y=(x.C) |
|---|---|---|---------|---------|
| 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 0 |



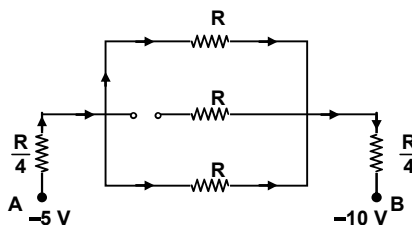
4. $V_{RB} = 500 \text{ K}\Omega \times 10 \text{ MA} = 5 \text{ V}$
 $\therefore V_{BE} = 5.5 - 5 = 0.5 \text{ V}$

5. (i) $V_A = -10 \text{ V}$ and $V_B = -5 \text{ V}$
 Diodes D_1 and D_3 are reverse biased D_2 is forward biased.

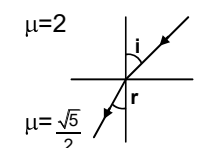


$$\Rightarrow R_{AB} = R + \frac{R}{4} + \frac{R}{4} = \frac{3}{2}R$$

- (ii) When $V_A = -5 \text{ V}$ and $V_B = -10 \text{ V}$
 Diodes D_2 is reverse biased D_1 and D_3 are forward biased.



$$\Rightarrow R_{AB} = \frac{R}{4} + \frac{R}{2} + \frac{R}{4} = R$$

6. If β is fringe width, then $7.5 \beta = 7.5 \text{ mm}$ (given)
 $\lambda = 5000 \text{ \AA}$
7. $\tan \theta_1 = \frac{B_V}{B_H \cos \alpha}, \tan \theta_2 = \frac{B_V}{B_H \sin \alpha}$
 $\Rightarrow \frac{\tan \theta_1}{\tan \theta_2} = \tan \alpha$
8. Plate A, C, E at same potential
 $\Rightarrow C_{\text{EFF}} = \frac{\epsilon_0 A}{d}$
 $\therefore U = \frac{1}{2} \frac{\epsilon_0 A}{d} V^2$
9. $\frac{kq'}{R} + \frac{kq}{r} = 0$
 $q' = -\left(\frac{R}{r}\right)q = -\left(\frac{R}{3R}\right) \times 10 = -10 \mu\text{C}$
10. $P_0(\pi r^2) + \text{weight of liquid above sphere.}$
11. $\omega' = \sqrt{\frac{K}{m} - \frac{b^2}{4m^2}}$
12. $V = 0$, Since the x-axis is equidistant.
13. Speed of belt
 $v = \omega r = 20 \times 0.2 = 4 \text{ m/sec}$
 $a_b = \mu g = 5 \text{ m/sec}^2$
 $\therefore s = \frac{V^2}{2a} = 1.6 \text{ m}$
 Work done by friction = $\mu mg \times 1.6 = +16 \text{ J}$
14. Net force on current carrying loop kept in a uniform magnetic field is always zero.
 For $\alpha = 0$, torque = 0
- 15.
- 
- $2 \sin i = \frac{\sqrt{5}}{2} \sin r$
 $\Rightarrow \tan r = \frac{4}{3}$
 $\therefore \hat{f} = \frac{-4\hat{i} - 3\hat{j}}{5}$
16. For $V_1 < 5 \text{ volt}$ the diode is forward biased output will be fixed at 5 V and $V_1 > 5 \text{ volt}$ the diode is reverse biased, and output will follow V_1 .

18. From the F.B.D. of the body

$$a = \frac{V\rho_1 g - V\rho g}{V\rho_1} = \left(1 - \frac{kh}{\rho_1}\right)g \quad \because \rho = kh$$

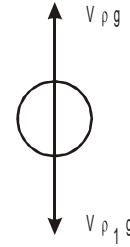
$$\therefore v \frac{dv}{dh} = \left(1 - \frac{kh}{\rho_1}\right)g$$

$$\Rightarrow \frac{v^2}{2} = \left(h - \frac{k}{2\rho_1}h^2\right)g$$

$$\therefore v = 0 \text{ at } h = \frac{2\rho_1}{k}$$

also $a = 0 \Rightarrow h = \frac{\rho_1}{k}$ is the mean position.

$$\therefore \text{amplitude} = \frac{\rho_1}{k}$$



19. $V_A = V_C = V_0\sqrt{2}$ m/s
 $V_B = 2V_0$ m/s

$$\therefore KE = \frac{1}{2}2m(2V_0)^2 + \frac{1}{2}m(\sqrt{2}V_0)^2 + \frac{1}{2}3m(\sqrt{2}V_0)^2 + \left[\frac{1}{2}mV_0^2 + \frac{1}{2}mR^2 \times \frac{V_0^2}{R^2}\right] = 9mV_0^2$$

20. $KE = \frac{3}{2}KT$, $V_{\text{rms}} = \sqrt{\frac{3RT}{M}}$

$$\text{i.e. } \frac{KE_2}{KE_1} = \frac{T_2}{T_1} = 2$$

$$\therefore KE_2 = 2KE_1 = 2 \times 6.21 \times 10^{-21} \\ = 12.42 \times 10^{-21} \text{ J}$$

$$\frac{V_{\text{rms},2}}{V_{\text{rms},1}} = \sqrt{\frac{T_2}{T_1}} = \sqrt{2}$$

$$\Rightarrow V_{\text{rms},2} = \sqrt{2} \times V_{\text{rms},1} = 684 \text{ m/s.}$$

21. from the theory

23. $Q = C^2 \left[m_{\text{nuc}} \left({}^A_Z X \right) - m_{\text{nuc}} \left({}^A_{Z-1} Y \right) - m_{e^+} \right]$ by definition.

Putting,

$$m_{\text{nuc}} \left({}^A_Z X \right) = m \left({}^A_Z X \right) - Zm_e$$

and similarly for ${}^A_{Z-1} Y$,

we get the final result.

24. $T = Kx = m\omega^2 r$

where $r = \ell_0 + x$

$$\therefore Kx = m\omega^2(\ell_0 + x) \Rightarrow x = \frac{m\omega^2 \ell_0}{K - m\omega^2}$$

$$\therefore r = \ell_0 + x = \frac{K\ell_0}{K - m\omega^2}$$

25. $6I = I^2 R + I^2 R$

$$\Rightarrow 3 = IR; V = 3 \therefore I = 9A$$

$$\Rightarrow R = \frac{1}{3} \Omega.$$

26. Impulse = Force \times time; net momentum of the system is conserved as the net force on it is zero.

27. Total internal energy of system will remain conserve

$$nC_{V_1}T_1 + nC_{V_2}T_2 = [nC_{V_1} + nC_{V_2}]T$$

$$\left(\frac{3}{2}R\right)300 + \left(\frac{5R}{2}\right)600 = \left[\frac{3R}{2} + \frac{5R}{2}\right]T$$

$$T = \left(\frac{9+30}{8}\right)100 = \frac{3900}{8} = 487K \text{ (approx)}$$

$$\Delta E = \left(\frac{3}{2}R\right)[487 - 300] = 187 \times \frac{3}{2} \times R = 280.5 R$$

28. The gravitational potential at a point Q (OQ = x) is given by :

$$V(x) = \begin{cases} -g_s R \left(\frac{3}{2} - \frac{1}{2} \frac{x^2}{R^2} \right), & \text{when } x < R \\ -g_s R \left(\frac{R}{x} \right), & \text{when } x > R \end{cases}$$

The energy required to project the body, to a maximum altitude of 3R from its surface, is :

$$m \left(V_B \Big|_{x=\frac{R}{2}} - V_P \Big|_{x=4R} \right) = \frac{9}{8} mg_s R.$$

29. B (at P) = $2 \cdot \frac{\mu_0 i}{2\pi r} \cdot \sin \theta$

30. $\sin \theta_C = \frac{2\mu}{3}$

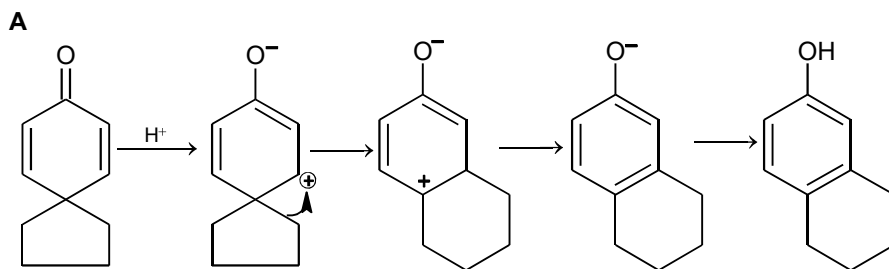
At face AC, i is 60°

$i > \theta_C$

CHEMISTRY (PART-II)

- B**
Conceptual
- D**
Conceptual
- C**
Syn Addition
- C**
Due to greater +R effect
- C**
Grignard addition at ketone followed by neighbouring group participation
- C**
Greater be the steric hinderance lesser be the rate of S_N2
- B**
 S_N2 reaction
- C**
(i) Wittig reaction (ii) HBO

9.



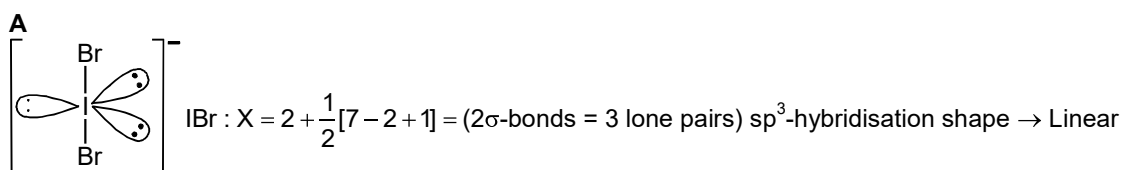
10.

A
Crossed aldol condensation

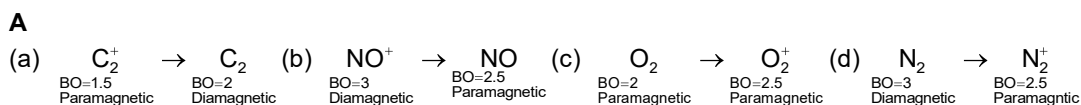
11.

C
Electronic configuration is ns^2np^3 , as fifth ionisation energy is unusually as compared to fourth one

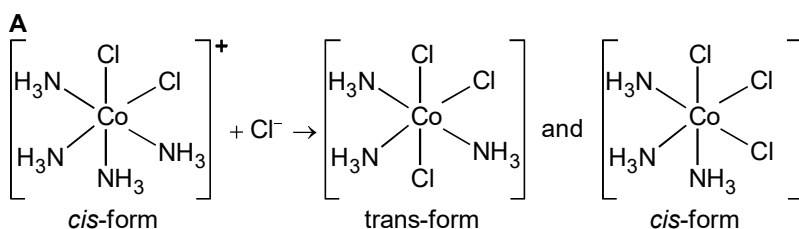
12.



13.



14.



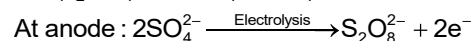
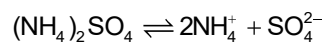
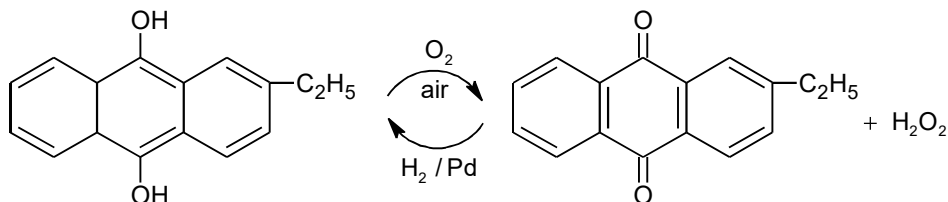
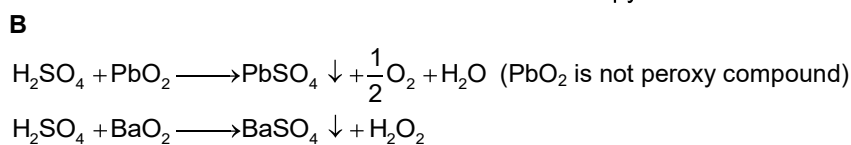
15.

D
Conceptual

16.

C
Reducing character $\propto \frac{1}{\text{'E-H' bond dissociation enthalpy}}$

17.



Peroxo sulphate on hydrolysis, produces H_2O_2 .

18.

B
Conceptual

19. **C**
Conceptual
20. **A**
The six-membered cyclic ether is known as pyranose while the five membered cyclic ether is known as furanose. Linkage at C-1 carbon of α -glycosidic linkage in carbohydrate chemistry.
21. **A**
Conceptual
22. **B**
As the process is isothermal
23. **B**
Conceptual
24. **A**
As $\text{Ag} + \text{I}^- \longrightarrow \text{AgNO}_3$
Final concentration of $\text{I}^- = 0.25 \text{ M}$ (As 0.25 mol yellow ppt is formed)
- $$\text{I}_2 + \text{I}^- \rightleftharpoons \text{I}_3^-$$
- | | | | |
|---------|------|------|------|
| t = 0 | 1 | 0.5 | |
| t = teq | 0.75 | 0.25 | 0.25 |
- $$K = \frac{[\text{I}_3^-]}{[\text{I}_2][\text{I}^-]} = \frac{0.25}{0.75 \times 0.25} = \frac{1}{.75} = 1.33$$
25. **A**
 $[\text{H}_2\text{CO}_3] = 1 \text{ M}$
 $[\text{H}^+] = [\text{HCO}_3^-]$
 $K_{a_1} = \frac{[\text{H}^+][\text{HCO}_3^-]}{[\text{H}_2\text{CO}_3]}$ $[[\text{H}_2\text{CO}_3] \approx 1 \text{ M as } K_{a_1} \text{ is small}]$
 $K_{a_1} = [\text{H}^+]^2$
 $[\text{H}^+] = \sqrt{K_{a_1}} = 2 \times 10^{-3}$
26. **A**
Effective no of O^{2-} per unit cell = 4
Effective no of Zn^{2+} per unit cell = 1
Effective no of Al^{3+} per unit cell = 2
Formula of spinel = ZnAl_2O_4
27. **D**
Force of attraction between solute and solvent molecule decreases after dissolution
28. **D**
 $\frac{[\text{Cl}]}{[\text{Cl}_2]} = K_{\text{eq}}$
 $[\text{Cl}] = [K_{\text{eq}}[\text{Cl}_2]]^{1/2}$
rate = $K_2[\text{Cl}][\text{CHCl}_3]$
= $K_3 K_{\text{eq}}[\text{Cl}_2]^{1/2}[\text{CHCl}_3]$
29. **D**
Negative sol will form because KI is in excess.
30. **B**
No of nodal surface = $n - \ell - |m| = 5 - 0 - 1 = 4$

MATHEMATICS (PART-III)

1. We know that if $d_i = \frac{x_i - A}{h}$ then $\sigma_x = |h|\sigma_d$

$$\text{In this case } -2x_i - 3 = \frac{x_i + \frac{3}{2}}{-\frac{1}{2}}$$

$$\text{So, } h = -\frac{1}{2}$$

$$\text{Then } \sigma_d = \frac{1}{|h|}\sigma_n = 2 \times 3.5 = 7$$

2. Apply L' Hospital's Rule

$$2xf(x) = (1 + x^2) f'(x) \Rightarrow \frac{f'(x)}{f(x)} = \frac{2x}{1+x^2}$$

$$\lim_{x \rightarrow 1} \frac{\ln f(x) - \ln 2}{x - 1} \left(\frac{0}{0} \right) = \lim_{x \rightarrow 1} \frac{2x}{1+x^2} = 1$$

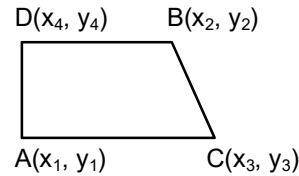
3. On solving we have

$$(x_1 - x_3)^2 + (x_2 - x_4)^2 + (y_2 - y_3)^2 + (y_1 - y_4)^2 \leq 0$$

$$\Rightarrow x_1 = x_3, x_2 = x_4, y_2 = y_3 \text{ and } y_1 = y_4$$

$$\Rightarrow \frac{x_1 + x_2}{2} = \frac{x_3 + x_4}{2} \text{ and } \frac{y_1 + y_2}{2} = \frac{y_4 + y_3}{2}$$

Hence AB and CD bisect each other
Also we have $AB^2 = CD^2$
 $\Rightarrow AB = CD$



4. Constructing the truth table we get the answer.

		a	b	x	y	z	Opt A	Opt B	Opt C	Opt D
p	q	$p \rightarrow q$	$\sim q$	$a \wedge b$	$a \wedge q$	$\sim p$	$x \rightarrow z$	$x \rightarrow p$	$y \rightarrow z$	$y \rightarrow p$
T	T	T	F	F	T	F	T	T	F	T
T	F	F	T	F	F	F	T	T	T	T
F	T	T	F	F	T	T	T	T	T	F
F	F	T	T	T	F	T	T	F	F	T

5. To have the area to be less than the circumference, we need to have the diameter be either 2 or 3.

$$\text{The possible ways to roll a 2 or 3 is 3, therefore the answer being } \frac{3}{36} = \frac{1}{12}$$

6. Let $W = \{CAT, TOY, YOU, \dots\}$

Clearly, R is reflexive and symmetric but not transitive
Since $CAT R TOY, TOY R YOU \not\Rightarrow CAT R YOU$

7. We must have $x^2 + x - 6 \neq 0$ and $\left[x + \frac{1}{2} \right] > 0, \left[x + \frac{1}{2} \right] \neq 1$

$$\Rightarrow x \neq -3, 2 \text{ and } \left[x + \frac{1}{2} \right] \geq 2$$

$$\Rightarrow x + \frac{1}{2} \geq 2$$

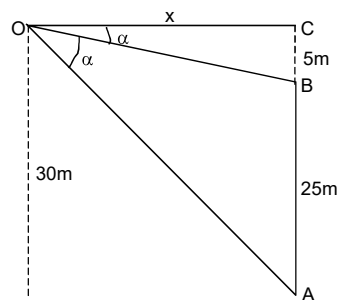
$$\Rightarrow x \geq \frac{3}{2}$$

$$\Rightarrow x \in \left[\frac{3}{2}, 2 \right) \cup (2, \infty)$$

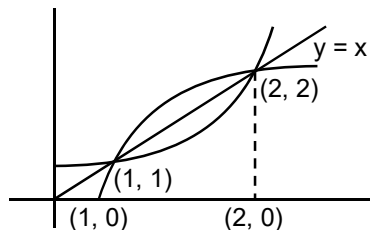
8. On solving, we get $(p - q)^2 + (p - 1)^2 + (q - 1)^2 = 0$
 $\Rightarrow p, q = 1$
 Putting the values of p and q , $\Delta = 0$ as elements are in AP

9. Let the middle point of chord be (h, k)
 \therefore equation of chord is $T = S_1$
 $\Rightarrow 3xh - 2yk + 2(x + h) - 3(y + k) = 3h^2 - 2k^2 + 4h - 6k$
 Slope of this chord = $\frac{3h+2}{2k+3} = 2$ (given)
 $\Rightarrow 3h - 4k = 4$
 \therefore Locus is $3x - 4y = 4$

10. We have $\tan \alpha = \frac{5}{x}$ and $\tan 2\alpha = \frac{30}{x}$
 $\Rightarrow \tan 2\alpha = \frac{30}{5 \cot \alpha}$
 $\Rightarrow \tan 2\alpha = 6 \tan \alpha \Rightarrow 3 - 3 \tan^2 \alpha = 1$
 $\Rightarrow \tan \alpha = \sqrt{\frac{2}{3}} \Rightarrow x = 5 \cot \alpha = 5\sqrt{\frac{3}{2}}$ m



11. Area = $2 \left| \int_1^2 x dx - \int_1^2 (x^2 - 2x + 2) dx \right| = \frac{1}{3}$ square



12. $\log_2(1 + \sqrt{6x - x^2 - 8}) \geq 0$
 $\Rightarrow 1 + \sqrt{6x - x^2 - 8} \geq 1 \Rightarrow 6x - x^2 - 8 \geq 0$
 $\Rightarrow x^2 - 6x + 8 \leq 0$
 $\Rightarrow (x - 2)(x - 4) \leq 0$
 $\Rightarrow 2 \leq x \leq 4$.

Now $f'(x) = x^2 + 2x + 2 > 0 \forall x \in \mathbb{R}$
 $\Rightarrow f(x)$ is strictly increasing in $[2, 4]$

$$f(x) = \frac{x^3}{3} + x^2 + 2x + c$$

$$\alpha = f(2) = \frac{8}{3} + 4 + 4 + c = \frac{32}{3} + c$$

$$\beta = f(4) = \frac{64}{3} + 16 + 8 + c = \frac{136}{3} + c$$

$$|\alpha - \beta|_{\max} = \frac{104}{3}$$

13. $A = \begin{bmatrix} 5 & -2 \\ -7 & 3 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 0 & 4 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 2 & -1 \end{bmatrix} = \begin{bmatrix} -16 & 3 \\ 24 & -5 \end{bmatrix}$

14. $E_1 \Rightarrow$ Person is accident person
 $E_2 \Rightarrow$ Person is not accident person
 $A =$ person will have an accident with in a year
 $P(A) = P(E_1)P(A/E_1) + P(E_2)P(A/E_2) = 0.3 \times 0.6 + 0.7 \times 0.8 = 0.74$

15. Let $\frac{1}{H_{i+1}} - \frac{1}{H_i} = k$

$$\sum_{i=1}^{2n} (-1)^i \left(\frac{H_i + H_{i+1}}{H_i - H_{i+1}} \right) = \sum_{i=1}^{2n} \frac{(-1)^i}{k} \left(\frac{1}{H_{i+1}} + \frac{1}{H_i} \right) = 2n$$

16. $T_{r+1} = {}^{12}C_r \left(3^{\frac{1}{4}} \right)^{12-r} \cdot (4)^{r/3} = {}^{12}C_r \cdot 3^{(3-r/4)} \cdot (4)^{r/3}$

For rational term $r = 0$ or 12

$$\therefore \text{Sum} = T_1 + T_{13} = {}^{12}C_0 \cdot 3^3 + {}^{12}C_{12} \cdot 4^4 = 3^3 + 4^4 = 27 + 256 = 283$$

17. $-1 \leq x^2 - 10x + 26 \leq 1 \Rightarrow x = 5$ only and at $x = 5$

$$\frac{\pi}{2} = 0 \text{ which not possible. Hence } a \in \phi.$$

18. for $5 \leq f(a) < 6 \times [f(x)] = 5$
Hence cont. at $x = a$

19. $I = \int \sin(100x + x) \cdot (\sin x)^{99} dx$
 $= \int (\sin(100x)\cos x + \cos 100x \cdot \sin x) (\sin x)^{99} dx$
 $= \int \underbrace{\sin(100x)\cos x}_{\text{i}} \cdot \underbrace{(\sin x)^{99}}_{\text{ii}} dx + \int \cos(100x) \cdot (\sin x)^{100} dx$
 $= \frac{\sin(100x)(\sin x)^{100}}{100} - \frac{100}{100} \int \cos(100x)(\sin x)^{100} dx + \int \cos(100x)(\sin x)^{100} dx$
 $= \frac{\sin(100x)(\sin x)^{100}}{100} + C$

20. D.R's of normal to plane $x + y + z - 1 = 0$ and $x + ky + 3z - 1 = 0$ is $(1, 1, 1)$ and $(1, k, 3)$ respectively
 \Rightarrow D.R. of normal to a plane perpendicular to given planes

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 1 \\ 1 & k & 3 \end{vmatrix} = \hat{i}(3-k) - \hat{j}(2) + \hat{k}(k-1)$$

$$\Rightarrow \frac{1+2\lambda}{3-k} = \frac{2+\lambda}{-2} = \frac{1+3\lambda}{k-1} \Rightarrow -2-4\lambda = 6+3\lambda-2k-\lambda k \text{ and } -2-6\lambda = -2-\lambda+2k+\lambda k$$

$$-4-10\lambda = 4+2\lambda \Rightarrow 12\lambda = -8 \Rightarrow \lambda = -\frac{2}{3}$$

$$\Rightarrow -2 + \frac{8}{3} = 6 - 2 - 2k + 2 - k = 3 \Rightarrow \frac{2}{3} - 4 = -\frac{4}{3}k \Rightarrow -\frac{10}{3} = -\frac{4}{3}k \Rightarrow k = \frac{5}{2}$$

21. $x^n + \alpha x + \beta = (x - \alpha_1)^2 (x - \alpha_2) \dots (x - \alpha_{n-1})$

$$\Rightarrow \frac{x^n + \alpha x + \beta}{(x - \alpha_1)^2} = (x - \alpha_2)(x - \alpha_3) \dots (x - \alpha_{n-1})$$

$$\Rightarrow (\alpha_1 - \alpha_2)(\alpha_1 - \alpha_3) \dots (\alpha_1 - \alpha_{n-1}) = \lim_{x \rightarrow \alpha_1} \left(\frac{x^n + \alpha x + \beta}{(x - \alpha_1)^2} \right) = \frac{n(n-1)}{2} \cdot \alpha_1^{n-2}$$

22. Favourable cases

X	Y
GGGGG	BBB
BBBGG	GGG

$$\Rightarrow \text{Required probability} = \frac{{}^5C_5}{{}^8C_5} + \frac{{}^5C_3}{{}^8C_3} = \frac{11}{56}$$

23. Put $n = \frac{1}{x}$

$$\lim_{x \rightarrow 0} \frac{1}{x} \left\{ \frac{1}{x} \ln \left(\frac{1}{1+x} \right) + 1 \right\} = \lim_{x \rightarrow 0} \frac{1}{x} \left\{ 1 - \frac{\ln(1+x)}{x} \right\} = \lim_{x \rightarrow 0} \left(\frac{x - \left(x - \frac{x^2}{2} + \frac{x^3}{3} - \dots \right)}{x^2} \right) = \frac{1}{2}$$

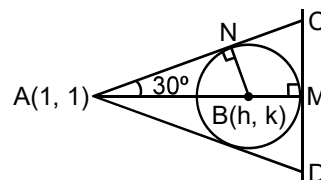
24. Let co-ordinates of centre are B(h, k)

$$BN = BM$$

$$AB \sin 30^\circ = BM$$

$$\sqrt{(h-1)^2 + (k-1)^2} \cdot \frac{1}{2} = \frac{|2h+4k-5|}{\sqrt{20}}$$

$$11k^2 - h^2 + 16hk - 10h - 30k + 15 = 0.$$



25. Length of focal chord making an angle α with x-axis is $4a \operatorname{cosec}^2 \alpha$

For $\alpha \in \left(0, \frac{\pi}{4} \right]$, it's minimum length = $(4a)(2) = 8a$

26.
$$T_n = \frac{n}{n^2 + k^2 x^2} = \frac{1}{n \left(1 + \left(\frac{k}{n} \right)^2 x^2 \right)}$$

$$S = \frac{1}{n} \sum_{k=1}^n \frac{1}{1 + \left(\frac{k}{n} \right)^2} = \int_0^1 \frac{dt}{1 + t^2 x^2} = \frac{1}{x^2} \int_0^1 \frac{dt}{t^2 + \left(\frac{1}{x^2} \right)} = \left[\frac{1}{x} \tan^{-1} tx \right]_0^1 = \frac{\tan^{-1} x}{x}$$

27. $(\vec{b} \times \vec{c}) \cdot (\vec{a} \times \vec{d}) = (\vec{b} \cdot \vec{a})(\vec{c} \cdot \vec{d}) - (\vec{b} \cdot \vec{d})(\vec{c} \cdot \vec{a})$

Using above formula.

28. $\frac{dy}{dx} = 2ax = 2x \left(\frac{y}{x^2} \right); \frac{dy}{dx} = \frac{2y}{x}$

$$\text{Now, } m \frac{dy}{dx} = -1 \Rightarrow m = -\frac{x}{2y} \Rightarrow \frac{dy}{dx} = -\frac{x}{2y}; y^2 = -\frac{x^2}{2} + c$$

29. Complex number z is in 4th quadrant

So, principal value of $\arg(z)$ will be $-\tan^{-1} \left| \tan \frac{4\pi}{5} \right|$.

30. $f(x) = \cos^{-1} x + \tan^{-1} x$

$$f'(x) = \frac{-1}{\sqrt{1-x^2}} + \frac{1}{1+x^2}$$

$$f''(x) = -x \left\{ \frac{1}{(1-x^2)^{3/2}} + \frac{2}{(1+x^2)^2} \right\}$$

$$\Rightarrow f'(x) \leq 0$$